

**ACADEMIA INTERNATIONAL
CONFERENCE ON MATHEMATICS AND
MATHEMATICS EDUCATION**

**“NEW TRENDS IN MATHEMATICS AND MATHEMATICS
EDUCATION”**

1-3 December 2021, Siirt, TURKEY

ISBN: 978-625-00-0578-1

Chairman of the Organizing Committee

Prof. Dr. Ali AKGÜL

Assist. Prof. Enes DEMİR

Assist. Prof. Seda İĞRET ARAZ

Dear Respected Academics and Researchers,

Online Presentations:

On behalf of the Organizing Committee, we are pleased to announce that the First Academia International Conference on Mathematics and Mathematics Education (AICMME-2021) will be held in Siirt University from 25-27 November 2021. Due to the COVID-19 pandemic, presentations will be held online. This conference focuses on the theory and the applications of all mathematical sciences. All researches related to Pure Mathematics/Mathematics Education are in the scope of the conference topics. AICMME -2021 provides an ideal academic platform for researchers and professionals to discuss current and universal issues in both mathematics and mathematics education sciences and share their experiences. You can find more information about this event on the AICMME -2021 website:

All articles undergo rigorous peer-review by at least two scientific committee members or additional reviewers. While conference languages are in English and Turkish, short abstracts and proceedings should be prepared in English.

All registered participants will be given a certificate of participation and sent by e-mail.

We look forward to seeing you in Siirt/ Turkey.

With our best regards,

Organizing Committee of AICMME-2021

Halil Coşkun ÇELİK, Siirt University

Mustafa OBAY, Siirt University

Ramazan KAMA, Siirt University

Esra KARATAŞ AKGÜL, Siirt University

Abdulkadir KARAKAŞ, Siirt University

Rukiye ŐAMCI KARADENİZ, Siirt University

İlyas KARADENİZ, Siirt University

Malik DURMAZ, Siirt University

İrem AKBULUT ARIK, Siirt University

Furkan ÖZDEMİR, Siirt University

Yusuf ALAGÖZ, Siirt University

Sibel Yasemin GÖLBOL, Siirt University

Kamer ARSLAN, Siirt University

Scientific Committee

Prof. Dr. Abdon Atangana, University of Free State, South Africa

Prof. Dr. Dumitru Baleanu, Çankaya University, Turkey

Prof. Dr. Zakia Hammouch, Moulay İsmail University, Morocco

Prof. Dr. Thabet Abdeljawat, Prince Sultan University, Saudi Arabia

Prof. Dr. Jordan Hristov, University of Chemical Technology and Metallurgy, Bulgaria

Prof. Dr. Ali Akgül, Siirt University, Turkey

Prof. Dr. David Grow, Missouri University of Science and Technology, USA

Prof. Dr. Hijaz Ahmad, University of Engineering and Technology, Pakistan

Prof. Dr. Sadullah Jafarov, Muş University, Turkey

Prof. Dr. Emile Franc DOUNGMO GOUFO, University of South Africa, South Africa

Prof. Dr. Kottakkaran Sooppy Nisar, Prince Sattam bin Abdulaziz University, Saudi Arabia

Prof. Dr. Harun Polat, Muş University, Turkey

Prof. Dr. Cemil Tunç, Van University, Turkey

Prof. Dr. Fevzi Erdoğan, Van University, Turkey

Prof. Dr. Hacı Mehmet Baskonus, Harran University, Turkey

Prof. Dr. Mehmet Gıyas Sakar, Van University, Turkey

Prof. Dr. Mir Sajjad Hashemi, University of Bonab, Iran

Prof. Dr. Muhammad Imran Asjad, University of Management and Technology Lahore, Pakistan

Prof. Dr. Engin Özkan, Erzincan University, Turkey

Asst. Prof. Dr. Seda İğret Araz, Siirt University, Turkey

Prof. Dr. Jagdev Singh, JECRC University, India

Prof. Dr. Behzad Ghanbari, Kermanshah University of Technology, Iran

Prof. Dr. Talat Körpınar, Muş University, Turkey

Prof. Dr. Mustafa İnç, Elazığ University, Turkey

Prof. Dr. Hasan Bulut, Elazığ University, Turkey

Prof. Dr. Abdullah Kopuzlu, Atatürk University, Turkey

Prof. Dr. Hossein Jafari, University of South Africa, South Africa

Prof. Dr. Fahd Jarad, Çankaya University, Turkey

Prof. Dr. Nehad Ali Shah, Department of Mathematics, Lahore Leads University, Lahore, Pakistan

Prof. Dr. Mahmoud Abdel-Aty, Sohag University, Egypt

Prof. Dr. Tanfer Tanrıverdi, Harran University, Turkey
Prof. Dr. Mikail Et, Fırat University, Turkey
Prof. Dr. Yavuz Altın, Fırat University, Turkey
Prof. Dr. Murat Subaşı, Atatürk University, Turkey
Prof. Dr. Ahmet Ocak Akdemir, Ağrı University, Turkey
Prof. Dr. Qaseem Al-Mdallal, United Arab Emirates University, United Arab Emirates
Prof. Dr. Ahmet Şükrü Özdemir, Marmara University, Turkey
Prof. Dr. Zülbiye Toluk Uçar, İzzet Baysal University, Turkey
Prof. Dr. Kemal Özgen, Dicle university Turkey
Prof. Dr. Imran Siddique Department of Mathematics University of Management and Technology, Lahore, Pakistan
Assoc. Prof. Dr. Esra Karatas Akgül, Siirt University, Turkey
Assoc. Prof. Dr. Kenan Yıldırım, Muş University, Turkey
Asst. Prof. Dr. Ahmet Sazak, Muş University, Turkey
Assoc. Prof. Dr. Erdal Korkmaz, Muş University, Turkey
Assoc. Prof. Dr. Muhammet Çınar, Muş University, Turkey
Prof. Dr. Mohammed Al-Refai, Yarmouk University, Jordan
Asst. Prof. Dr. Serkan Aracı, Hasan Kalyoncu University, Turkey
Assoc. Prof. Dr. Mehmet Başkonuş, Harran University, Turkey
Assoc. Prof. Dr. Abdullah Aydın, Muş University, Turkey
Asst. Prof. Dr. Demet Deniz Yılmaz, Muş University, Turkey
Asst. Prof. Dr. Fatma Cumhuri, Muş University, Turkey
Asst. Prof. Dr. Altaf Khan, Abdul Wali Khan University, Pakistan
Assoc. Prof. Dr. Mahmut Modanlı, Harran University, Turkey
Asst. Prof. Dr. Muhsin İncesu, Muş University, Turkey
Dr. Kashif Ali Abro, Mehran University of Engineering and Technology, Pakistan
Assoc. Prof. Dr. Hülya Durur, Ardahan University, Turkey
Asst. Prof. Dr. Arzu Aykut, Atatürk University, Turkey
Asst. Prof. Dr. Melek Gözen, Van University, Turkey
Asst. Prof. Dr. Hakkı Güngör, Ufuk University, Turkey
Asst. Prof. Dr. Muhammad Farman, The University of Lahore, Pakistan
Asst. Prof. Dr. Abdulgani Şahin, Ağrı University, Turkey
Asst. Prof. Dr. Nesrin Manav, Erzincan University, Turkey
Asst. Prof. Dr. Erdal Eker, Muş University, Turkey

Assoc. Prof. Dr. Muhammad Bilal Sehole, University of Management and Technology, Pakistan

Dr. Kolade M. Owolabi, Federal University of Technology, Nigeria

Prof. Dr. Ebenezer Bonyah, Department of Mathematics Education, Ghana.

Asst. Prof. Dr. Rubab Manzoor, UMT University, Pakistan

Asst. Prof. Dr. Amir Khan ,University of Swat, Pakistan

Prof. Dr. Cemil Tunç, Van University, Turkey

Asst. Prof. Dr. Onur Saldır, Van University, Turkey

Asst. Prof. Dr. Fatih Özbağ, Harran University, Turkey

Prof. Dr. Malik Muhammad Abbas, Sargodha University, Pakistan

Prof. Dr. Abdullah Kablan, Gaziantep University, Turkey

Dr. Nurbige Turan Zabut, Gaziantep University, Turkey

Dr. Khurram Shabir, Government College University, Pakistan

Dr. Hatice Kübra SarıI, Atatürk University, Turkey

Dr. Öznur Özaltın, Hacettepe University, Turkey

Dr. Nourhane Attia University M'hamed Bougara of Boumerdes, Boumerdes, Algeria

Dr. Boutarfa Bariza, Professor of Physics, Guelma University, Algeria

Asst. Prof. Dr. Nauman Ahmed, The University of Lahore, Lahore, Pakistan

Prof. Dr. Muhammad Ozair Ahmad, The University of Lahore, Lahore, Pakistan

Prof. Dr. Muhammad Aziz-ur Rehman, University of Management and Technology, Lahore, Pakistan

Assoc. Prof. Dr. Muhammad Rafiq, University of Central Punjab, Lahore, Pakistan.

Dr Ali Raza, National College of Business and Administration, Lahore, Pakistan.

Asst. Prof. Dr. Muhammad Sajid Iqbal, The University of Lahore, Lahore, Pakistan.

Asst. Prof. Dr. Tahira Sumbal Shaikh, Lahore College for Women University, Lahore, Pakistan

Asst. Prof. Dr. Zafar Iqbal, The University of Lahore, Lahore, Pakistan.

Asst. Prof. Dr. Naveed Shahid, The University of Lahore, Lahore, Pakistan.

Asst. Prof. Dr. Muhammad Jawaz, The University of Lahore, Lahore, Pakistan.

Dr. Javaid Ali, GCT, Punjab Higher Education Department, Lahore, Pakistan.

Contents

On the search and study of analytical solutions of Generalized Differential Equations.....	1
A numerical study of initial flow past a circular cylinder subject to a circular motion.....	2
Developing Mathematics Literacy through Dual Focus Teaching.....	3
New Horizons in Digital Mathematics Teaching.....	4
On the fractal dynamics for higher order traveling waves.....	5
A numerical approach for solving distributed-order fractional Volterra-Fredholm Integro-Differential Equations.....	6
Monotonicity analysis for fractional difference operators.....	7
A Rubric Study for Evaluation of Mathematics Lesson Plans.....	8
Piecewise modeling: Applications to Nature.....	15
Investigation of The Effect of Game-Based Mathematics Teaching On Students' Motivations to Learn Mathematics.....	17
On f -Statistical convergence of order β of difference sequences of fractional order.....	20
An Examination of 12th Grade Students' Understanding of Central Trend And Difference Measures According to Solo Taxonomy.....	23
Reflections on an In-service Training Program Designed for.....	26
The Views of Some Participants of a Workshop on PWW's.....	27
Teaching based on 5E learning model's effect on the mathematics achievement and mathematical thinking skills of 7th grade students.....	28
Examination of secondary school students' mathematical metacognitive awareness according to some variables.....	30
On the existence of periodic solutions of a nonlinear functional differential equation.....	31
Predicting Mathematics Achievement: The Role of Mathematical Metacognition and Problem-Posing Self-Efficacy.....	32
Examining Preservice Elementary Mathematics Teachers' Pedagogical Content Knowledge on Patterns in Terms of Students' Errors.....	34
Examination of Teacher's Opinions on Teaching Multiplication Tables.....	35
Some Recent Development in OCDMA system and mathematical modeling.....	36
Impact of information and Lévy noise on stochastic COVID-19 epidemic model.....	37
A Fractional Mathematical Model of the ongoing Coronavirus Disease (COVID-19) Pandemic: A Case Study in Thailand.....	38
Power series representing posets.....	39
On the Stability of Nonlinear of Neutral Integro-Differential Equations.....	40

A Uniformly Convergent Difference Scheme for Singularly Perturbed Fredholm Integro-Differential Equation on Shishkin Mesh.....	42
A new family of the k - ζ -Fibonacci polynomials.....	44
A fractional mathematical model of tumor virus dynamics and treatment using virotherapy.....	47
Numerical solution of a fractional model of Covid-19 spread with non-total immunity.....	49
Transfer Functions by New General Integral Transform.....	51
The cubic B-spline polynomials approach for numerical solutions of Bagley-Torvik and Painlevé differential equations involving the Caputo-Fabrizio derivative.....	52
Reliable Structure Preserving Numerical Analysis of Epidemic Models.....	53
Applications of Lie groups and Lie algebras in numerical methods.....	54
Optimal balls of classical and stochastic systems of nonlinear partial differential equations.....	56
Application of Fractional Order Techniques on Diabetes Model.....	59
Numerical Analysis of a Non-Linear Stochastic Epidemic Model.....	60
Dynamical Behaviour of Smoking Model.....	61
Analysis of system of differential equations.....	62
Fractional stochastic inequalities involving p-convex stochastic process.....	63
Numerical Solutions of a Heat Transfer for Fractional Maxwell Fluid Flow with Water Based Clay Nanoparticles; A Finite Difference Approach.....	64
Weber-Type Integral Transform Connected with Robin-Type Boundary Conditions.....	65
Application of fractional derivatives.....	66

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

On the search and study of analytical solutions of Generalized Differential Equations

Juan E. Napoles Valdes^{1,2}

¹Universidad Nacional del Nordeste FaCENA, Corrientes Capital, 3400, Argentina

²Universidad Tecnológica Nacional FRRE, Resistencia, Chaco 3500, Argentina

Abstract

In this paper, we present some results related to obtaining and studying the solutions of generalized differential equations, by means of a certain generalized integral transformation. The results obtained in the first part of the work are illustrated with two general cases: a generalized differential equation, which contains as a particular case a non-conformal differential equation previously studied by the author, in terms of its oscillatory nature, and a partial differential equation conformable, of Klein Gordon type. Some difficulties and errors in the global fractional case are presented.

AMS Subject Classification (2010): Primary 26A33, Secondary 34K37.

Key words and phrases: Fractional derivatives e integral, generalized derivative, fractional calculus.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

A numerical study of initial flow past a circular cylinder subject to a circular motion

Qaseem Al-Mdallal¹

¹Department of Mathematical Sciences, United Arab Emirates University

Abstract

This presentation focusses on a numerical treatment of the initial flow past a circular cylinder with combined streamwise and transverse oscillations. The motion is governed by the two-dimensional unsteady Navier–Stokes equations in non-primitive variables. The method of solution is based on the perturbation theory together with the collocation method. The development of the physical properties of the flow such as time at which the fluid separates, drag and lift coefficients at early times is captured. Comparisons with existing results verify the accuracy of the present results.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Developing Mathematics Literacy through Dual Focus Teaching

Murat ALTUN¹

¹Uludağ University Department of Mathematics Education, Turkey

Abstract

Developing Mathematical Literacy with a Dual-Focus Teaching Model

A) What is Mathematical Literacy? Its Evaluation in terms of Mathematical Literacy in Turkey

B) Dual Focus Teaching Model

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

New Horizons in Digital Mathematics Teaching

Aslan GÜLCÜ¹

¹Atatürk University Department of Mathematics Education, Turkey

Abstract

Digital Immigrants are creating new neighborhoods, villages, cities and perhaps new countries. Virtual migration, which started especially after the 2000s, continues to affect social life deeply. New generations, such as the Z generation, where immigrants are raised, are born and grow up in virtual worlds. With these characteristics, each generation becomes a person of a different world. Every new generation has the opportunity to learn, perceive, transfer, live, etc. human characteristics also vary according to the characteristics of the generation. As such, the 'features' of the previous generation cease to be the 'features' of the next generation and become archaic.

On the fractal dynamics for higher order traveling waves

Emile F. Doungmo Goufo¹

¹Department of Mathematical Sciences, University of South Africa, Florida, 0003, South Africa.

Abstract

Auto replication processes remain fascinating in sciences, engineering and technology as their applications in machining/biological systems have been widely used to solve number of outstanding problems in communities' every day lives. Finding innovative techniques capable of generating auto replication processes in various fields has then become the priority for number of scientists. One of those fields includes wave motion. In this paper, we use the 7th order Korteweg-de Vries (KdV) model, combined with the fractal-fractional operator to artificially (numerically) generate auto replication processes characterizing the evolution of higher order traveling waves. The well-posedness for the combined model is first studied with the establishment of its existence and uniqueness results. We also explore other dynamics related to notions such as the Dubai highway and the triniton. Numerical simulations then follow and prove that the higher order traveling wave together with other dynamics can be involved in a self replication process.

**A numerical approach for solving distributed-order fractional Volterra-Fredholm
Integro-Differential Equations**

H. Jafari^{1,2,*}, R.M. Ganji¹, M.N. Ncube²

¹Department of Mathematical Sciences, University of South Africa, UNISA 0003, South
Africa

² Department of Mathematics, University of Mazandaran, Babolsar, Iran

*Presenter: jafari.usern@gmail.com

Abstract

In this work, a numerical method is presented to obtain approximate solution of distributed-order integro-differential equations. The approximate solution is expressed in the form of a polynomial with unknown coefficients and in place of differential and integral operators, we make use of matrices that we deduce from the shifted Legendre polynomials. To compute the numerical values of the polynomial coefficients, we set up a system of equations that tallies with the number of unknowns, we achieve this goal through the Legendre-Gauss quadrature formula and the collocation technique. The theoretical aspects of the error bound is discussed.

Keywords: Distributed-Order Integro-Differential Equations; Operational Matrix; The Legendre-Gauss Quadrature; Volterra-Fredholm Integro-Differential Equations.

Monotonicity analysis for fractional difference operators

Thabet Abdeljawad¹

¹Department of Mathematics and Sciences, Prince Sultan University, Saudi Arabia

Abstract

Discrete fractional monotonicity analysis discusses the relation between the sign of the fractional difference operators, either in nabla or delta sense, and the monotonicity of the discrete function under investigation. We investigate the monotonicity coefficient of different kernel type discrete fractional difference operators in the power, exponential and Mittag-Leffler laws, and for the proportion discrete fractional case. As an application different versions of the Mean Value Theorem are formulated for such types of discrete fractional calculus. Comparisons are made to understand the structure of such classes of discrete fractional operators.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

A Rubric Study for Evaluation of Mathematics Lesson Plans

İnayet ÖZEL*

ozellinyt@gmail.com

*Siirt University Department of Mathematics Education, Siirt, Turkey

Cahit PESEN

cahit.pesen@gmail.com

*Siirt University Department of Mathematics Education, Siirt, Turkey

Malik DURMAZ*

malikdurmaz@gmail.com

*Siirt University Department of Mathematics Education, Siirt, Turkey

Abstract

Though societies are evaluated based on education to see their level of development, teacher competence is what is taken as a criterion for the quality of education as teacher competence is one of the crucial factors that affects the quality of teaching. Although teacher competencies are defined as a construct consisting of two dimensions: "understanding and enactment" (Park & Oliver, 2008, p.278) and "continuity" (Blömeke et al. 2015, p.8), they can be defined as the set of knowledge, skills, attitudes, and values required for teachers to teach in various situations (MEB, 2017; Weinert, 2001). In order to train teachers with high levels of competence, it is essential to develop and evaluate the competencies possessed by pre-service teachers while receiving pre-service education. One of the competencies that should be developed and evaluated in terms of the level of development is education and training planning (MEB, 2017). Being aware of the gains that are aimed to be gained by the student; mastering the learning-teaching methods, techniques and strategies to be used in gaining the gains; organizing materials to match student characteristics and teaching process; Situations such as student foreknowledge, being aware of the mistakes, difficulties and solution suggestions that can be experienced in teaching are the components of education and training planning competence. Although planning education and training may seem like a discrete teacher competence, it is a competence that co-ordinates many of the teacher competences

identified. Components of the competence to plan education and training include awareness of the acquisitions which are targeted for the student, a good command of the learning-teaching methods, techniques, and strategies to be employed in gaining the acquisitions, organization of the materials in compliance with the student characteristics and teaching process, previous knowledge of the student, awareness of the mistakes, difficulties, and solution suggestions that may be experienced in teaching. Although education and training planning may seem like a discrete teacher competence, it is a competence that co-ordinates many of the teacher competences identified.

An important part of education and training planning involves designing lesson plans. While designing the lesson plan, almost all of the components involved in the education and training planning competence are used. The lesson plan increases the quality of teaching (Bilen, 2002; Kablan, 2012) and the level of success (Konyalıođlu, Konyalıođlu, & Iřık, 2002; Kablan, 2012) as it is a guide that determines the functioning in the teaching process (Özaltun Çelik & Bukova Güzel, 2017). It is crucial to develop and evaluate the competence of preparing a lesson plan as it is not only related to other competencies and but also a competence in itself. While field education courses taught in pre-service education serve to develop this competence, there is also a need for a measurement tool to be employed for the evaluation of lesson plans. In this context, this study seeks to develop a lesson plan evaluation rubric to evaluate lesson plans designed by pre-service teachers.

In the first part of the rubric development process, the relevant literature (Bilen, 2002; Jones, 2005; Ball, Sleep, Boerst, & Bass, 2009; Özaltun Çelik & Bukova Güzel, 2017) was reviewed and criteria for the evaluation of lesson plans were identified. The goal was to create a rubric by writing score specifications for the identified criteria. An expert opinion form (in form of “it is appropriate” and “it is not appropriate” was created to submit the rubric to the expert opinion. The consensus rates of the experts ranged between 0.5 and 1. Experts also expressed their opinions in writing. In line with the opinion of the first round of the expert opinion, it was observed that the criteria and specifications of the rubric needed to be arranged and the rubric was submitted to the expert opinion for the second time with the arrangements made. In the second round, the expert consensus rate was calculated as 1. This value indicates a perfect fit for consensus (Şencan, 2005). In this way, the validity of the rubric was ensured by both the literature and expert opinion (Yıldırım & Şimşek, 2013). The rubric obtained after the second round of expert opinion was applied on 42 lesson plans prepared by the pre-service teachers within the scope of the geometry and measurement teaching course. To test the reliability of the rubric, two raters independently evaluated the lesson plans. The Spearman

Brown Rank Differences coefficient between these evaluations was calculated and found ranging between 0.608 and 1.00. A rater training session was held to eliminate the inconsistency between raters following this implementation. Along with the rater training, minor arrangements were made for some of the criteria and specifications of the rubric, and the rubric took its final shape. After this session, 43 lesson plans prepared by pre-service teachers who took geometry and measurement teaching lessons were evaluated according to the final version of the rubric. The Spearman Brown Rank Differences correlation coefficient between raters for this assessment was calculated between 0.786 and 1.00. As a result, it can be suggested that the relevant lesson plan evaluation rubric is a reliable measurement tool.

In this study, a rubric was developed to evaluate lesson plans. The relevant rubric consists of three parts: imprint, functioning, and assessment-evaluation. In the imprint part, there are 11 criteria including the name of the course, grade level, subject(s), recommended course duration, learning area, sub-learning area, acquisitions, skills, learning-teaching methods and techniques, tools and materials/materials used, terms or concepts. In the functioning part, there are 9 criteria including readiness, ability to gain terms or concepts, misconceptions, being acquisition-oriented and skills-oriented, compatibility with learning-teaching methods and techniques, use of materials, roles of teacher and student, appropriateness of the language used. The assessment and evaluation part consists of 4 criteria including suitability for learning outcomes, suitability for functioning, conceptual suitability of evaluation elements, and suitability of evaluation elements in terms of grammar. The rubric can create a total score through weighting of the criteria and thus, normative studies are required. Studies can be conducted to meet this requirement. In future studies, lesson plans can be evaluated through this rubric and thus, this rubric used as an argument for measuring teacher competence. On the other hand, the specifications of the criteria can also be used as a feedback tool.

Keywords: Teacher Competence, Lesson Plan Evaluation, Rubric Development, Lesson Plan Evaluation Rubric, Mathematics Teaching.

References

- Ball, D., Sleep, L., Boerst, T. & Bass, H. (2009). Combining the development of practice and the practice of development in teacher education, *The Elementary School Journal*, 109(5), 458-474.
- Bilen, M. (2002). *Plandan Uygulamaya Öğretim*, Anı Yayıncılık, Ankara.

- Blömeke, S., Gustafsson, J. E. & Shavelson, R. J. (2015). Beyond dichotomies: competence viewed as a continuum, *Zeitschrift für Psychologie*, 223(1), 3-13.
- Jones, K. (2005). Planning for mathematics learning. In S. Johnston-Wilder, P. Johnston-Wilder, D. Pimm & J. Westwell, (Ed.). *Learning to Teach Mathematics in the Secondary School (2nd ed.)* (93-113). London: GB. RoutledgeFalmer.
- Kablan, Z. (2012). Öğretmen adaylarının ders planı hazırlama ve uygulama becerilerine bilişsel öğrenme ve somut yaşantı düzeylerinin etkisi, *Eğitim ve Bilim*, 37(163), 239-253.
- Konyalıoğlu, A.C., Konyalıoğlu, S. & Işık, A. (2002). Matematik derslerinde planlı eğitim üzerine, *Kastamonu Eğitim Dergisi*, 10(2), 351-358.
- MEB. (2017). *Öğretmenlik mesleği genel yeterlikleri*, Öğretmen Yetiştirme ve Geliştirme Genel Müdürlüğü, Ankara.
- Özaltun Çelik, A. & Bukova Güzel, E. (2017). Matematik öğretmenlerinin ders imecesi kapsamında köklü ifadelerin öğretimine ilişkin oluşturdukları ders planı, *Mersin Üniversitesi Eğitim Fakültesi Dergisi*, 13(2): 561-594.
- Park, S. & Oliver, J. S. (2008). Revisiting the conceptualisation of pedagogical content knowledge (PCK): PCK as a conceptual tool to understand teachers as professionals, *Research in Science Education*, 38(3), 261-284.
- Şencan, H. (2005). *Sosyal Ve Davranışsal Ölçümlerde Güvenilirlik Ve Geçerlilik*, Seçkin Yayıncılık, Ankara, 499-559.
- Yıldırım, A. & Şimşek, H. (2013). *Sosyal Bilimlerde Nitel Araştırma Yöntemleri*, Seçkin Yayınevi, Ankara.
- Weinert, F. E. (2001). Concept of Competence: A Conceptual Clarification. In D. S. Rychen & L. H. Salganik, (Ed.). *Defining and Selecting Key Competencies* (45-65). Seattle, WA: Hogrefe and Huber Publishers.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

**Examination of high school 10th grade students' proof skills in context of mathematical
reasoning**

Enes DEMİR

Siirt University Department of Mathematics Education, Siirt, Turkey

(ORCID: 0000-0002-9012-8109)

Mail: enesdemir@siirt.edu.tr

Gamze IRAZ

Siirt University Department of Mathematics Education, Siirt, Turkey

Mail: gamze.iraz@hotmail.com

Abstract

In mathematics education, the method of showing the correctness of theorems and rules and convincing people is reasoning and proof, which is the heart and soul of mathematics, with its feature of reaching various generalizations or results in an axiomatic system. Based on this importance, the aim of the study is to examine the proof-making skills of high school 10th grade students in the mathematical context. One of the basic building blocks of mathematics is proof. The importance of the concept of proof is increasing day by day with the thought that the power of mathematical thinking comes from proof. Many studies conducted today show that students have low success in proving and have difficulties. Although the concept of proof may seem like a simple mathematical operation, it has more than one function in its infrastructure. In order for a student to perform a mathematical operation and reach the result, he must first understand the given operation, then examine it, make logical inferences and move on to the solution phase. With this study, it was tried to determine which stages the students used while proving, at which stage they had the most difficulty, and how well they had mastered the mathematical terms, what kind of reasoning mistakes they made. In this context, the study was carried out with a total of 60 students studying at different high schools in a city in Turkey. As a data collection tool in the study, 4 scenario-type proofs were asked,

which were formed from the literature and expert opinion appropriate to the levels of high school students. The data obtained were categorized with the reasoning errors detection scale. As a result of the analysis, it was revealed that high school students made reasoning mistakes such as accepting a special case as a proof, creating invalid proofs, using the language of mathematics correctly, inconsistency between proof steps, and they had many difficulties in writing proofs. Based on the results of this study, it is suggested that the high school curriculum requires more proving to be included and that more studies should be conducted on this.

Keywords: Proof, reasoning, mathematics education, high school students

References

- Almeida, D. (2003). Engendering proof attitudes: Can the genesis of mathematical knowledge teach us anything? *International Journal of Mathematical Education in Science and Technology*, 34(4), 479-488.
- Baki, A. (1999). Öğretmen eğitimi üzerine düşünceler. *Türk Yurdu*, 19(138), 4-9.
- Boero, P. (1999). Argumentation and mathematical proof: A complex, productive, unavoidable relationship in mathematics and mathematics education. *International Newsletter on the Teaching and Learning of Mathematical Proof*. Retrieved February 16, 2021 from <http://www.lettredelapreuve.org/OldPreuve/Newsletter/990708Theme/990708ThemeUK.html>
- Cai, J., & Cirillo, M. (2014). What do we know about reasoning and proving? Opportunities and missing opportunities from curriculum analyses. *International Journal of Educational Research*, 64, 132–140.
- CadwalladerOlsker, T. (2011). What do we mean by mathematical proof? *Journal of Humanistic Mathematics*, 1(1), 33-60.
- Öztürk, T. (2020, March). Matematğin kalbi: İspat [The heart of mathematics: Proof]. APSİSTEK. <https://www.apsistek.com/index.php/mart-2020/178-matematigin-kalbi-ispata>
- Petrou, M., & Goulding, M. (2011). Conceptualising teachers' mathematical knowledge in teaching. In T. Rowland & K. Ruthven (Eds.), *Mathematical knowledge in teaching* (pp. 9–25). Springer.

Perry, P., Molina, Ó., Camargo, L., & Samper, C. (2011, February). Analyzing the proving activity of a group of three students. Paper presented at Congress of the European Society for Research in Mathematics Education (CERME 7), Poland.

Piecewise modeling: Applications to Nature

Seda İĞRET ARAZ¹

¹sedaaraz@siirt.edu.tr, Siirt University, Faculty of Education, Department of Mathematics
Education, Siirt, Turkey.

Abstract

In this study, we present some applications of a new concept called the piecewise derivative, which is useful in depicting different processes at different time intervals, such as power law, fading memory, classical. For applications, we consider well-known the logistic equation and present some applications of such model. Also, we deal with Van Der Pol equation which can be used for modeling heart rhythm of a human. We present numerical simulations different behaviors of heart rhythm and different patterns of logistic equation via piecewise concept.

Keywords: Piecewise differential operators, logistic equation, heart rhythm model.

References

- [1] Verhulst, P.-F. "Recherches mathématiques sur la loi d'accroissement de la population." *Nouv. mém. de l'Academie Royale des Sci. et Belles-Lettres de Bruxelles* **18**, 1-41, 1845.
- [2] Verhulst, P.-F. "Deuxième mémoire sur la loi d'accroissement de la population." *Mém. de l'Academie Royale des Sci., des Lettres et des Beaux-Arts de Belgique* **20**, 1-32, 1847.
- [3] Lian J., Krätschmer H., Müssig D., Open Source Modeling of Heart Rhythm and Cardiac Pacing, *The Open Pacing, Electrophysiology & Therapy Journal*, 2010, 3, 28-44.
- [4] Caputo, M., Fabrizio M., A New Definition of Fractional Derivative Without Singular Kernel, *Progress in Fractional Differentiation and Applications*, 1(2015),2, pp.73-85.

- [5] Atangana A., Baleanu D., New fractional derivatives with non-local and non-singular kernel: Theory and Application to Heat Transfer Model, *Thermal Science*, 20 (2), 2016, 763-769.
- [6] A Atangana, S·I Araz, New concept in calculus: Piecewise differential and integral operators, *Chaos, Solitons & Fractals* 145, 110638, 2021.
- [7] Atangana A, Araz SI., New numerical scheme with Newton polynomial: Theory, Methods, and Applications, Academic Press, 978-0323854481, 2021.
- [8] Balakrishnan M., Chakravarthy VS., Guhathakurta S., Simulation of Cardiac Arrhythmias Using a 2D Heterogeneous Whole Heart Model, *Frontier in Physiology*, 2015.
- [9] Trayanova NA., Tice BM., Integrative computational models of cardiac arrhythmias.simulating the structurally realistic heart, *Drug Discov Today Dis Models*, 2009, 6(3): 85.91.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

**Investigation of The Effect of Game-Based Mathematics Teaching On Students'
Motivations to Learn Mathematics**

Enes DEMİR

Siirt University Department of Mathematics Education, Siirt, Turkey

Mail: enesdemir@siirt.edu.tr

Mert ARAR

Siirt University Department of Mathematics Education, Siirt, Turkey

Mail: mertarar1@gmail.com

Abstract

Mathematics lessons are one of the most important lessons in terms of gaining many important qualities such as creative, original, critical thinking, reasoning, problem solving and so on. Therefore, as a requirement of being an information society, it is necessary to create an effective and efficient mathematics teaching-learning environment in schools and other educational institutions. One of these methods can be provided with game-based mathematics education. Mathematics and games take their place in the life of the individual at different levels, with different functions and contents. In mathematics, reaching advanced abstractions and generalizations from simple concrete relations takes place at advanced levels with time and the development of the individual. In the game, the types of games played by the development of the individual differ. As time passes, the individual who encounters different situations in the game acquires different skills and develops himself. Many mathematical experiences are experienced in the game, which is a serious occupation of the child. Play is a developmental opportunity built on real-life experiences, where the foundations of mathematical thinking are laid. Based on this importance, the aim of the study is to examine the effect of game-based mathematics education on students' motivation to learn mathematics.

In line with the purpose of the study, he worked with 7th grade students (22+22) in primary education. In the study, using the quasi-experimental method, the students were divided into control group and experimental group. The researcher himself conducted the lessons of both groups. While the game-based mathematics teaching was carried out in the experimental group, the lessons were taught with the existing teaching methods and techniques in the control group. When both the post-test data and the clinical interviews with the students and the observation data made during the lessons were examined, it was determined that the teaching of mathematics with games contributed positively to the motivation of the students, and the students showed more interest in participating in the lessons more actively. It is suggested that more work should be studied on game-based mathematics teaching.

Keywords: Game, mathematics education, motivation, primary education

References

- Açıköz, K. Ü. (2003). Aktif Öğrenme. İzmir: Eğitim Dünyası Yayınları, 6. Basım
- Altıparmak, K. ve Öziş, T. 2005. Matematiksel ispat ve matematiksel muhakemenin gelişimi üzerine bir inceleme. Ege Eğitim Dergisi, 6(1), 25-37.
- Anderson, T., Shattuck, J. (2012). Design-based research: A decade of progress in education research? Educational researcher, 41(1), 16-25.
- Charles, M., Bustard, D., & Black, M. (2009). Experiences of promoting engagement in game-based learning. Proceedings of the European Conference on Games Based Learning, 397-403. Retrieved from Education Research Complete database
- Creswell, J.W. (2014). Araştırma deseni: Nitel, nicel ve karma yöntem yaklaşımları (Çev. Ed. S. B. Demir). Ankara: Eğiten Kitap.
- Çimen, E. E. (2008). Matematik öğretiminde, bireye “Matematiksel Güç” kazandırmaya yönelik ortam tasarımı ve buna uygun öğretmen Etkinlikleri geliştirilmesi. Doktora Tezi. Dokuz Eylül Üniversitesi Eğitim Bilimleri Enstitüsü, İzmir.
- Dağdelen, S., ve Ünal, M. (2017). Matematik öğrenim ve öğretim sürecinde karşılaşılan sorunlar ve çözüm önerileri. Yüzüncü Yıl Eğitim Fakültesi Dergisi, 14, 483-510.

- Hays, R.T.(2005).The effectiveness of instructional games: a literature review and discussion.
- Katmada, A., Mavridis, A., & Tsiatsos, T. (2014). Implementing a gam efor supporting learning in mathematicss. The Electronic Journal of e-Learning, 12(3), 230-242.
- Kaya, S. & Elgün, A. (2015). Eğitsel oyunlar ile desteklenmiş fen öğretiminin ilkokul öğrencilerinin akademik başarısına etkisi. Kastamonu Eğitim Dergisi. 23(1), 329-342
- Kuzu, A., Çankaya, S., Mısırlı, Z. A. (2011). Tasarım tabanlı araştırma ve öğrenme ortamlarının tasarımı ve geliştirilmesinde kullanımı. Anadolu Üniversitesi Eğitim Bilimleri Enstitüsü Dergisi, 1(1), 19-35.
- Milli Eğitim Bakanlığı [MEB]. (2013). Ortaöğretim matematik dersi (1,2,3, 4. sınıflar) öğretim programı. Ankara: MEB Yayınları.
- Moore, R. C. (1994). Making the transition to formal proof. Educational Studies in Mathematics, 27, 249-266.
- National Council of Teachers of Mathematics [NCTM]. (2000). Principles and standards for school mathematics. Reston, VA: Author.
- Tural, H. (2005). İlköğretim matematik öğretiminde oyun ve etkinliklerle öğretimin erişi ve tutuma etkisi. Yayınlanmamış Yüksek Lisans Tezi. D.E.Ü., Eğitim Bilimleri Enstitüsü, İzmi

On f -Statistical convergence of order β of difference sequences of fractional order

Abdulkadir KARAKAŞ

Department of Mathematics, Siirt University, Siirt -TURKEY

E-mail: kadirkarakas21@hotmail.com

Abstract

In this work, we introduce the concept of f -statistical convergence of order α by using fractional difference operator Δ_p^α and investigate its properties. Some topological properties for this space are presented and some inclusion relations are established.

Keywords: Difference operators, Statistical Convergence, Sequence spaces, Fractional difference operators.

References

- [1] Aizpuru, A. Listán-García, M. C. and Rambla-Barreno, F. Density by moduli and statistical convergence, *Quaest. Math.* 37(4) (2014) 525--530.
- [2] Altin, Y. Properties of some sets of sequences defined by a modulus function, *Acta Math. Sci. Ser. B Engl. Ed.* 29(2) (2009), 427--434.
- [3] Baliarsingh, P. Some new difference sequence spaces of fractional order and their dual spaces. *Appl. Math. Comput.* 219 (2013), no. 18, 9737--9742.
- [4] Baliarsingh, P.; Dutta, S. On the classes of fractional order difference sequence spaces and their matrix transformations. *Appl. Math. Comput.* 250 (2015), 665--674.
- [5] Bektaş, Ç. A.; Et, M.; Çolak, R. Generalized difference sequence spaces and their dual spaces. *J. Math. Anal. Appl.* 292 (2004), no. 2, 423—432.
- [6] Bhardwaj, V. K.; Dhawan, S. f - statistical convergence of order α and strong Cesàro summability of order α with respect to a modulus, *J. Inequal. Appl.* (2015), 332, 14 pp.
- [7] Bhunia, S.; Das, P. and Pal, S. K. Restricting statistical convergence, *Acta Math. Hungar.* 134(1-2) (2012), 153--161.
- [8] Connor, J. S. The statistical and strong p -Cesàro convergence of sequences, *Analysis* 8 (1988), 47-63.
- [9] Çolak, R. Statistical convergence of order α , *Modern Methods in Analysis and Its Applications*, Anamaya Pub., New Delhi, India (2010), 121-129.
- [10] Et, M. and Çolak, R. On some generalized difference sequence spaces, *Soochow J. Math.* 21 (4) (1995), 377-386.
- [11] Et, M. On some topological properties of generalized difference sequence spaces. *Int. J. Math. Math. Sci.* 24 (2000), no. 11, 785-791.

- [12] Et, M., Altinok, H. and Altin, Y. On some generalized sequence spaces, *Appl. Math. Comput.* 154 (1) (2004), 167-173.
- [13] Fast, H. Sur la convergence statistique, *Colloquium Mathematicum* 2 (1951), 241-244.
- [14] Fridy, J. On statistical convergence, *Analysis*, 5, 301-313, 1985.
- [15] Gadjiev, A. D. and Orhan, C. Some approximation theorems via statistical convergence, *Rocky Mountain J. Math.* 32(1) (2002), 129-138.
- [16] Gaur, A. K.; Mursaleen, M. Difference sequence spaces. *Internat. J. Math. Math. Sci.* 21(4), (1998), 701--706.
- [17] Ioan, T. On some p -convex sequences, *Acta Univ. Apulensis, Math. Inform.* 11 (2006), 249-257.
- [18] Işik, M. On statistical convergence of generalized difference sequences. *Soochow J. Math.* 30 (2) (2004), 197—205.
- [19] Karakaş, A. and Altın, Y. $\Delta_{\{p\}^{\{m\}}}$ -Statistical Convergence, 2. International Conference On Analysis and Its Applications, Abstract Book, ISBN: 978-605-85712-3-5, Ahi Evran University, Kırşehir / TURKEY - (2016). p. 43.
- [20] Karakaş, A.; Altin, Y. and Et, M. $\Delta_{\{p\}^{\{m\}}}$ -statistical convergence of order α . *Filomat* 32 (16), (2018), 5565--5572.
- [21] Kızmaz, H. On certain sequence spaces, *Canad. Math. Bull.* 24 (2) (1981), 169--176.
- [22] Kolk, E. The statistical convergence in Banach spaces, *Tartu ÜI. Toimetised* No. 928, (1991) 41--52.
- [23] Maddox, I. J. Sequence spaces defined by a modulus, *Math. Proc. Cambridge Philos. Soc.* 100 (1), (1986), 161--166.
- [24] Maddox, I. J. A new type of convergence, *Math. Proc. Cambridge Philos. Soc.* 83 (1), (1978), 61--64.
- [25] Malkowsky, E.; Parashar, S. D. Matrix transformations in spaces of bounded and convergent difference sequences of order m . *Analysis* 17 (1) (1997), 87--97.,
- [26] Malkowsky, Eberhard; Mursaleen, M.; Suantai, Suthep. The dual spaces of sets of difference sequences of order m and matrix transformations *Acta Math. Sin. (Engl. Ser.)* 23 (3) (2007), 521--532.
- [27] Mölder, A. The topologization of sequence spaces defined by a matrix of moduli, *Proc. Estonian Acad. Sci. Phys. Math.* 53 (4), (2004), 218--225.
- [28] Nakano, H. Concave modulars, *J. Math. Soc. Japan.* 5,(1953), 29-49.
- [29] Ruckle, W.H. FK- spaces in which the sequence of coordinate vectors is bounded, *Canad. J. Math.* 25,(1973), 973-978.
- [30] Šalát, T. On statistically convergent sequences of real numbers, *Math. Slovaca* 30 (1980), 139-150.

- [31] Schoenberg, I. J. The integrability of certain functions and related summability methods, Amer. Math. Monthly 66 (1959), 361-375.
- [32] Steinhaus, H. Sur la convergence ordinaire et la convergence asymptotique, Colloq Math. 2, (1951), 73-74.
- [33] Tabib, K. K. The Topology of Statistical Convergence, Master's Thesis, Department of Mathematical Sciences, The University of Texas at El Paso, August 2012, USA.
- [34] Tripathy, B. C. On generalized difference paranormed statistically convergent sequences, Indian J. Pure Appl. Math. 35(5) (2004), 655--663.
- [35] Zygmund, A. Trigonometric Series, Vol. I, II. Reprinting of the 1968 version of the second edition with Volumes I and II bound together. Cambridge University Press, Cambridge-New York-Melbourne., 1977.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

**An Examination of 12th Grade Students' Understanding of Central Trend And
Difference Measures According to Solo Taxonomy**

Enes DEMİR

Siirt University Department of Mathematics Education, Siirt, Turkey

Necmettin KORKMAZ

Siirt University Department of Mathematics Education, Siirt, Turkey

Abstract

In our society, where technology advances and spreads rapidly, information and data collection has an important place. With the increase in data collection and knowledge, people approach events from different perspectives and develop different solutions. Statistical knowledge and statistical thinking are needed in the process of evaluating and interpreting this information and data, which appear as graphics or tables in all areas of daily life. For this reason, the importance given to statistics has increased in the world and statistics subjects have taken their place in mathematics programs in many countries. The purpose of this research is to examine which meanings secondary school 12th grade students attribute to the measures of central tendency and diffusion and at what level these meanings are according to the SOLO Taxonomy. The study was conducted with 72 students who continue their education in the 12th grade in three different high schools (high, medium and low level according to academic success) in a city center in Turkey in the fall semester of the 2021-2022 academic year. 5 scenario-type questions were asked to reveal students' statistical thinking levels about central tendency and diffusion measures. In the preparation of these questions, the relevant literature was scanned and the questions were finalized by taking expert opinions. The data about the statistical thoughts of the students were obtained from the clinical interviews and the solutions of the students during the interview. The data obtained were analyzed with the descriptive analysis method under the qualitative paradigm within the framework of the Solo Taxonomy. According to the results obtained, the students' level of

understanding of central tendency measures such as range and standard deviation was low; It was observed that the level of understanding for the concept of "average" was high. The results of the study are thought to be a preliminary preparation for the studies to be carried out in this field.

Keywords: Statistical literacy, Solo Taxonomy, mathematics education, high school students

References

- Akkaş, E. N. (2009). 6.- 8. Sınıf Öğrencilerinin İstatistiksel Düşüncelerinin İncelenmesi. Abant İzzet Baysal Üniversitesi Sosyal Bilimler Enstitüsü İlköğretim Matematik Anabilim Dalı.
- Carmichael, C., Callingham, R., Watson, F. & Hay, J. (2009). Factors influencing the development of middle school students' interest in statistical literacy. *Statistics Education Research Journal*, 8(1), 62-81.
- Cerrito, P. B. (1999). Teaching statistical literacy. *College Teaching*, 47(1), 1-7.
- Chan, C. C., Tsui, M. S., Chan, M. Y. C. & Hong, H. J. (2002). Applying the Structure of the Observed Learning Outcomes (SOLO) Taxonomy on Student's Learning Outcomes: An empirical study. *Assessment & Evaluation in Higher Education*, 6(27).
- Cobb, G. W. (1992). Report of the joint ASA/MAA committee on undergraduate statistics. *In the American Statistical Association 1992 proceedings of the Section on Statistical Education*, (pp. 281–283). Alexandria, VA: American Statistical Association
- Gal, I. (2002). Adult statistical literacy: Meanings, components, responsibilities. *International Statistical Review*, 70(1), 1-25.
- Garfield, J., & Ben-Zvi, D. (2005, May). A framework for teaching and assessing reasoning about variability. *Statistics Education Research Journal*, 4(1), 92–99. Retrieved December 26, 2006, from [http://www.stat.auckland.ac.nz/~iase/serj/SERJ4\(1\)GarfieldBenZvi.pdf](http://www.stat.auckland.ac.nz/~iase/serj/SERJ4(1)GarfieldBenZvi.pdf)
- Groth, R. E., & Bergner, J. A. (2006). Preservice elementary teachers' conceptual and procedural knowledge of mean, median, and mode. *Mathematical Thinking and Learning*, 8, 37–63.

Howitt D. & Cramer, D. (1997). A guide to computing statistics with SPSS for Windows. Prentice Hall/Harvester Wheatsheaf, [ISBN 9780137291977](#)

Konold, C., & Higgins, T. (2003). Reasoning about data. In J. Kilpatrick, W. G. Martin & D. E. Schifter (Eds.), *A research companion to principles and standards for school mathematics* (pp. 193–215). Reston, VA: National Council of Teachers of Mathematics (NCTM).

Konold, C. & Pollatsek, A. (2002). Data analysis as the search for signals in noisy processes. *Journal for Research in Mathematics Education*, 33(4), 259–289.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Reflections on an In-service Training Program Designed for

Primary School Teachers

Ahmet ÇETİN, Ahmet DELİL, Bülent Nuri ÖZCAN, Mehmet Nuri ÖĞÜT, Metin GENÇAY,
Hüseyin DELİL, Mine AYYILDIZ, Semra NALBANTOĞLU ve Emine ATASOY ÖZTÜRK

Celal Bayar University Department of Mathematics Education, Turkey

Abstract

This is a cooperative in-service training program between Manisa Celal Bayar University (MCBU) Faculty of Education and Şehzadeler District Directorate of National Education. It is designed to contribute to the assessment and evaluation knowledge of primary school teachers, to determine the cognitive level of a fourth-grade primary school mathematics item according to TIMSS assessment framework, to write problems in accordance with this framework at each cognitive level, and to improve their competence by applying the written items in the classroom measurement and evaluation processes. The project entitled with “Developing My Professional Skills With TIMSS” was carried out between 29.01.2021 and 26.11.2021. In this talk, information about the in-service training program is given, including the views of the participants.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

The Views of Some Participants of a Workshop on PWW's

Ahmet DELİL

Celal Bayar University, Department of Mathematics Education, Turkey

Abstract

This study includes details on a workshop entitled “Proof without words in mathematics education” as a part of TUBITAK 2237-A project called “Proof applications in mathematics education”. The participants are graduate students from various universities in Turkey. In this study, we evaluate this workshop in the light of the participants’ views.

**Teaching based on 5E learning model's effect on the mathematics achievement and
mathematical thinking skills of 7th grade students**

Mehmet Şirin KURT^a , Halil Coşkun ÇELİK^b

^aMilli Eğitim Bakanlığı, Öğretmen, Diyarbakır, Türkiye.

E-mail: mehmetsirinkurt@gmail.com Orcid: 0000-0002-7155-5201

^bDoç. Dr. Siirt Üniversitesi, Eğitim Fakültesi, Matematik Eğitimi Anabilim Dalı, Siirt,
Türkiye.

E-mail: hcoskun.celik@gmail.com Orcid: 0000-0003-0056-5338

Abstract

In this study, it is aimed to examine the effect of teaching with the 5E Learning Model of the 7th grade algebra learning field on students' mathematics achievement and mathematical thinking skills. The research was carried out with 80 7th grade students in total including 40 experiment and 40 checking group students a public school in the Kayapınar district of Diyarbakır. The research was designed in a quasi-experimental design with pre-test post-test control group. Implementation part of the research lasted for 6 weeks. During the implementation process, the lessons were taught with the experimental group with the lesson plans developed according to the 5E Learning Model, while the lessons were taught according to the existing teaching methods in the control group. It is planned for the “achievement test of designing the data of the research for singular expressions” and thinking about mathematical thinking” independent samples t-test and dependent samples t-test were used in the analysis of the obtained data. As a result of the research, it was concluded that education with the 5E Learning Model increased the mathematics achievement of the students in the field of algebraic learning. There is a significant difference between the mean scores of students' mathematical thinking skills; It was determined that the effects of mathematical thinking were more in the experimental group than the students in the control group. It can be said that the 5E Learning Model makes a more positive contribution to the development of students' mathematical thinking skills. Although the examples of the 5E Learning Model in the field of mathematics are restricted, its applications in mathematics education give

successful results. Therefore, this model may increase its applications in other subjects in the field of mathematics training. It is hoped that these research findings will contribute significantly to better revealing the profiles of students in studies to be carried out based on 5E learning approaches.

Keywords: Mathematics achievement, Mathematics education, Mathematical thinking, Secondary school students.

**Examination of secondary school students' mathematical metacognitive awareness
according to some variables**

İsmail ARSLAN^a , Halil Coşkun ÇELİK^b

^aMilli Eğitim Bakanlığı, Öğretmen, Mardin, Türkiye. E-mail: ismailarslan@siirt.edu.tr Orcid: 0000-0002-6282-8095

^bDoç. Dr. Siirt Üniversitesi Eğitim Fakültesi, Matematik Eğitimi Anabilim Dalı, Siirt, Türkiye. E-mail: hcoskun.celik@gmail.com Orcid: 0000-0003-0056-5338

Abstract

In this study, secondary school students' mathematical metacognitive awareness were examined. It was examined whether there was a significant difference in terms of gender, class, socio-economic status of the family and education level of the parents on mathematics achievement. The research was carried out with a descriptive research model. The study was carried out on 462 (246 Girls, 216 Boys) students selected by convenient sampling method among secondary school students studying at 5th, 6th, 7th and 8th grades in a public school. "Personal Information Form" were used for the data collection tool and the "Mathematical Metacognition Awareness Scale" to reveal their mathematical metacognition awareness. Independent sample t-test, one-way analysis of variance were used in the analysis of the data. According to the results obtained from the research, it was found that students' mathematical metacognitive awareness were sufficient and at a high level. It was determined that students' mathematical metacognitive awareness differed significantly in terms of gender and mathematics achievement, but did not show a significant difference according to class, socio-economic status of the family, and education level of the parents. Activities to develop or increase students' awareness of mathematical metacognition should be prepared by paying attention to gender and mathematics achievement differences.

Keywords: Mathematical metacognition, Mathematics Achievement, Metacognitive awareness, Secondary school students

On the existence of periodic solutions of a nonlinear functional differential equation

İrem AKBULUT ARIK*, Cemil TUNÇ**

‡Siirt University, Faculty of Education, Department of Mathematics Education, Siirt, Turkey

**Yuzuncu Yil University, Faculty of Sciences, Department of Mathematics , 65080, Van, Turkey

Abstract

In this paper, we investigate the existence of periodic solutions of a nonlinear functional differential equation with variable delay. First, we transform the considered problem to an equivalent integral equation. Then, we define a fixed point mapping, which is written as a sum of contraction, and a compact map. Hence, we prove some results on the existence of periodic solution of the considered problem. The technique of the proofs depends on the Krasnoselskii's fixed point theorem. We give some examples for illustrations. By this work, we aim to do some contributions to the relevant topic and literature.

Keywords: Functional differential Equation, Fixed Point Theorem, Variable Delay.

References

- [1] Chen, G., Li,D., [Gaans, O.V., Lunel, S.V., 2018.](#) Stability results for nonlinear functional differential equations using fixed point methods. *Indag. Math. (N.S.)* [29, no. 2](#), 671–686.
- [2] Raffoul, Y.R., 2004. Stability in neutral nonlinear differential equations with functional delays using fixed point theory, *Mathematical and Computer Modelling* 40(7-8):691-700
- [3] Raffoul, Y. N., 2003. Periodic solutions for neutral nonlinear differential equations with functional delay, *Electron. J. Diff. Eqns.*, Vol. No. 102, 1–7.
- [4] Tunç, C., On the existence of periodic solutions of functional differential equations of the third order. *Appl. Comput. Math.* 15 (2016), no. 2, 189–199.
- [5] Tunç, C., New results on the existence of periodic solutions for Rayleigh equation with state-dependent delay. *J. Math. Fund. Sci.* 45 (2013), no. 2, 154-162.

**Predicting Mathematics Achievement: The Role of Mathematical Metacognition and
Problem-Posing Self-Efficacy**

Halil Coşkun ÇELİK^a , İsmail ARSLAN^b

^aDoç. Dr. Siirt Üniversitesi Eğitim Fakültesi, Matematik Eğitimi Anabilim Dalı, Siirt, Türkiye. E-mail: hcoskun.celik@gmail.com Orcid: 0000-0003-0056-5338

^bMilli Eğitim Bakanlığı, Öğretmen, Mardin, Türkiye. E-mail: ismailarslan@siirt.edu.tr Orcid: 0000-0002-6282-8095

Abstract

Metacognition is the ability of students to have knowledge about their own thinking processes and cognition and to organize this structure. Since metacognition is a method of discovering or choosing a specific mental process in the problem-solving process, it also has important effects on mathematical problem posing and achievement. This study explains the role of mathematical metacognitive awareness and problem posing in explaining mathematics achievement. In the study, middle school students' awareness of mathematical metacognition and self-efficacy in posing a mathematical problem were determined, and the relationship between them and their mathematics achievement was examined. The study, which was designed in the relational screening model, was conducted on 462 secondary school students. Data were collected through the “Problem Posing Self-Efficacy Scale” and the “Mathematical Metacognition Awareness Scale”. Pearson Product Moments Correlation coefficient and Multiple Linear Regression Analysis method were used to analyze the data. According to the results obtained from the study, a moderately significant relationship was found between students' mathematical metacognitive awareness and their self-efficacy in posing mathematical problems and their mathematics achievement. In addition, it was determined that students' mathematical metacognitive awareness and problem-posing self-efficacy predicted their mathematical success at the level of 35%. The results of this study point to the need to explore the importance of metacognition and problem posing as an important element in students' success in mathematics. The findings of the correlations between mathematical

metacognition, problem posing self-efficacy, and mathematics achievement suggest a possible focus for further research.

Keywords: Achievement, Mathematics education, Metacognition, Problem posing, Self-efficacy.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

**Examining Preservice Elementary Mathematics Teachers' Pedagogical Content
Knowledge on Patterns in Terms of Students' Errors**

Filiz Tuba DİKKARTIN ÖVEZ

Balıkkesir University Department of Mathematics Education Turkey

İlayda İNCE

Balıkkesir University Department of Mathematics Education Turkey

Abstract

The aim of this study is to examine primary school mathematics teacher candidates' pedagogical content knowledge about patterns in terms of student errors. 76 primary school mathematics teacher candidates studying in an education faculty in western Turkey and selected by convenient sampling method participated in the study. The study was based on case study, one of the qualitative research approaches. In order to collect the data of the study, the scale of "Pre-service Teachers' Knowledge of Students about Errors in the Subject of Patterns" developed by the researchers was used. Content analysis technique, one of the qualitative research methods, was used in the analysis and interpretation of the data. In the study, it was seen that the primary school mathematics teacher candidates did not have difficulty in detecting student mistakes and the reason for the error, their knowledge of recognizing pattern generalization strategies was high, and in this context, their pedagogical content knowledge about patterns was at a sufficient level. In addition, it was seen that they were more successful than quadratic patterns in finding the linear pattern rule, but they mostly made immature inductive reasoning while finding the pattern rule, and they were not at the desired level at Radford's algebraic generalization level.

Keywords: pattern, pedagogical content knowledge, error, pre-service mathematics teachers

Examination of Teacher's Opinions on Teaching Multiplication Tables

Cahit PESEN

Siirt University Department of Mathematics Education, Siirt, Turkey

Abstract

The aim of this research is to examine the views of teachers about multiplication table teaching and the multiplication table models used in teaching and to put forward suggestions for teaching based on the results. The multiplication table, which includes multiplication operations with one-digit natural numbers, is encountered by students starting from the 2nd grade of primary school. The process of learning the multiplication table is expected to be completed in the 3rd grade. Most primary school students make mistakes in simple multiplication or division operations because they have trouble learning the multiplication tables. This often leads to frustration, low self-esteem, lack of confidence and loss of interest in math.

Some Recent Development in OCDMA system and mathematical modeling

Kottakkaran Soopy Nisar¹

¹Department of Mathematics, Prince Sattam bin Abdulaziz University, Saudi Arabia

Abstract

The lustre of heuristic techniques inspires the researchers to develop computing infrastructures for handling the uncertainties that arise in the future prediction and control of COVID-19 spread virus, HIV infection of CD4+T cells model, Hantavirus model, HCV infection spread model, tumour growth model and other infectious diseases. Soft computing heuristics can handle the misleading situations in predicting and understanding the pandemic spread by designing the paradigms with more reliability, accuracy, precision and prediction of the bio-mathematics models. Based on the above fact, the recent development of mathematical modeling and its applications are considered in this talk.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Impact of information and Lévy noise on stochastic COVID-19 epidemic model

Anwarud Din¹

¹Department of Mathematics, Sun Yat-sen University, Guangzhou 510275, China

Abstract

In this paper, we consider the dynamical behavior of a stochastic coronavirus (COVID-19) epidemic model SIR with the inclusion of the influence of information intervention and Lévy noise. The existence and uniqueness of the model positive solution are proved. Then, we establish a stochastic threshold as a sufficient condition for the extinction and persistence in mean of the disease. Based on the available COVID-19 data, the parameters of the model were estimated and we fit the model with real statistics. Finally, numerical simulations are presented to support our theoretical results.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

**A Fractional Mathematical Model of the ongoing Coronavirus Disease (COVID-19)
Pandemic: A Case Study in Thailand**

Idris Ahmed¹

¹Department of Mathematics, Sule Lamido University, P. M. B 048 Kafin-Hausa, Jigawa
State, Nigeria.

Abstract

Since it was first identified in Wuhan, China, at the end of 2019, the coronavirus disease (COVID-19) pandemic has become a growing threat to global health. The epidemic emerged in Thailand in January 2020, with the Ministry of Public Health (MOPH) reporting the first cases in Bangkok. Mathematical modeling has been an effective method in understanding infectious disease transmission. In this paper, a compartmental epidemic model comprised of a system of six nonlinear differential equations with intervention strategy were propose and study to examines the transmission dynamics of the COVID-19 pandemic with reported data on daily cases of coronavirus in Thailand. The non-negativity and boundedness of the solutions were investigated, demonstrating that the model under consideration is mathematically and epidemiologically well-posed. Furthermore, using the concept of the next-generation matrix, we calculate the basic reproduction number and evaluate its stability. Furthermore, the proposed model was fitted with commutative and new daily cases from Thailand to validate and estimate some model parameters. To determine the impact of different parameters on R_0 , sensitivity analysis were investigated. To support the analytical results, an effective numerical scheme was employed to explore the dynamic behavior of the model.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Power series representing posets

Eric Dolores Cuenca^a, Jose Antonio Arciniega-Nevarez^b, Marko Berghoff^c

^aDivision de Ingenierias, Universidad de Guanajuato, Guanajuato, Mexico

^bMathematical Institute, University of Oxford, Oxford, UK

^cDepartment of mathematics, Yonsei University, Seoul, Korea

Abstract

In this work we rewrite the theory of order polynomials by using power series methods instead of polynomial methods. As a result we discover a non-recursive algorithm to compute the values of order polynomials of series-parallel posets. Given a power series $f(x)$, we describe an algorithm to recover, if possible, a poset whose order series is the power series $f(x)$. We introduce a family of posets, called Wixárika posets, and show that they satisfy a new variant of Stanley's reciprocity theorem. As an application we obtain new identities for binomial coefficients and properties of the negative hypergeometric distribution.

On the Stability of Nonlinear of Neutral Integro-Differential Equations

Melek Gözen

Department of Business Administration Faculty of Management Van Yuzuncu Yil
University 65080, Erciş –Van, TURKEY, E-mail: melekgozen2013@gmail.com

Cemil Tunc

Department of Mathematics Faculty of Sciences Van Yuzuncu Yil University 65080-
Kampus Van- Turkey, E-mail: cemtunc@yahoo.com

Abstract

This work deals with a nonlinear system of neutral delay integro-differential equations. Here, the asymptotic stability of solutions is studied. New results on the asymptotic stability of solutions are obtained by defining and using two new Lyapunov- Krasovskii functionals. The results of this paper generalize some former results and include them under weaker conditions. This paper also gives some new contributions to the theory of fundamental properties of solutions of neutral integro-differential equations.

Keywords: Asymptotic stability; Lyapunov functional; neutral integro-differential equations; linear matrix inequality

Mathematics Subject Classifications: 34K20; 34K40; 34K45; 93D30

References

- [1] Akbulut, I.; Tunç, C., On the stability of solutions of neutral differential equations of first order. *Int. J. Math. Comput. Sci.* 14 (2019), no. 4, 849–866.
- [2] Benhadri, M., Stability results for neutral differential equations by Krasnoselskii fixed point theorem. *Differ. Equ. Dyn. Syst.* 29 (2021), no. 1, 3–19.
- [3] Boyd, S.; El Ghaoui, L.; Feron, E.; Balakrishnan, V., Linear matrix inequalities in system and control theory. *SIAM Studies in Applied Mathematics*, 15. Society for Industrial and Applied Mathematics (SIAM), Philadelphia, PA.(1994)

- [4] Park, J. H.; Won, S., Stability analysis for neutral delay-differential systems. *J. Franklin Inst.* 337 (2000a), no. 1, 1–9.
- [5] Park, J. H.; Won, S., Stability of neutral delay-differential systems with nonlinear perturbations. *International Journal of Systems Science.* 31 (2000b), no. 8, 961-967.
- [6] Sun, L., Asymptotic stability for the system of neutral delay differential equations. *Appl. Math. Comput.* 218 (2011), no. 2, 337–345.
- [7] Tunç, C., Asymptotic stability of solutions of a class of neutral differential equations with multiple deviating arguments. *Bull. Math. Soc. Sci. Math. Roumanie (N.S.)* 57(105), (2014), no. 1, 121–130.
- [8] Tunç, C., Convergence of solutions of nonlinear neutral differential equations with multiple delays. *Bol. Soc. Mat. Mex. (3)* 21 (2015), no. 2, 219–231. *Ciencias Exactas, Físicas y Naturales. Serie A. Matemáticas* 15, no. 3, Article Number: 115.
- [9] Yang, M.; Liu, P., On asymptotic stability of linear neutral delay-differential systems. *Internat. J. Systems Sci.* 33 (2002), no. 11, 901–907.

**A Uniformly Convergent Difference Scheme for Singularly Perturbed Fredholm
Integro-Differential Equation on Shishkin Mesh**

Muhammet Enes DURMAZ,¹ Mustafa KUDU² and Gabil M. AMIRALIYEV²

¹Department of Information Technology, Kırklareli University, Kırklareli-TURKEY

²Department of Mathematics, Faculty of Science and Arts, Erzincan Binali Yıldırım
University, Erzincan-TURKEY

menesdurmaz025@gmail.com

muskud28@yahoo.com

gabilamirali@yahoo.com

Abstract

In the present study, the initial-value problem for a linear first-order singularly perturbed Fredholm integro-differential equation (SPFIDE) has been considered. By using interpolation quadrature rules and an exponential basis function, a difference scheme has been constructed with an accuracy of $O(N^{-2} \ln N)$ on a special non-uniform (Shishkin) mesh, where N is the mesh parameter. The difference scheme is demonstrated to be stable and convergent in the discrete maximum norm. The numerical example indicates that the proposed method has a convenient approach qualification.

References

- [1] G. M. Amiraliyev, M. E. Durmaz and M. Kudu, Uniform convergence results for singularly perturbed Fredholm integro-differential equation, *J. Math. Anal.*, 9(6), (2018), 55-64.

- [2] P. A. Farrel, A. F. Hegarty, J. J. H. Miller, E. O’Riordan and G. I. Shishkin, *Robust Computational Techniques for Boundary Layers*, Chapman and Hall/CRC, New York, 2000.
- [3] M. Kudu, I. Amirali and G. M. Amiraliyev, A finite-difference method for a singularly perturbed delay integro-differential equation, *J. Comput. Appl. Math.*, 308, (2016), 379-390.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

A new family of the k - ζ Fibonacci polynomials

Engin ÖZKAN¹ and Tuğba ALP²

¹Department of Mathematics, Faculty of Sciences and Arts, Erzincan Binali Yıldırım University, Yalnızbağ Campus, 24100, Erzincan, Turkey.

²Department of Mathematics, Graduate School of Natural and Applied Sciences, Erzincan Binali Yıldırım University, Yalnızbağ Campus, 24100, Erzincan, Turkey.

Abstract

The Fibonacci numbers, which have an important place today, appear not only in mathematics, but also in every aspect of our daily life. It is a number that is seen in nature, in the stock market, in the human body and in all areas of life and is associated with aesthetics.

The Fibonacci numbers, which have an increasing place in scientific studies and are the most well-known among the number sequences, first appeared in Leonardo Fibonacci's book 'Liber Abaci', which contains many basic problems, in a rabbit problem. Fibonacci numbers were obtained by writing down the total number of rabbits per month, with the new rabbits born by breeding only once a month, of a baby female and a male rabbit at the beginning. This sequence, which is obtained by adding the two numbers before it; It continues as 1,1,2,3,5,8,13,21,34,55,89,144,233,377,...

In this paper, we define a new family of k -Fibonacci Polynomials. We give the relationship between known Fibonacci Polynomials and k - ζ Fibonacci Polynomials. We present some properties and the matrix presentations of these polynomials. Finally, we give Cassini's identity for the polynomials.

Keywords: k -Fibonacci Numbers, k -Fibonacci Polynomials, Cassini Identity, a Matrix Generator.

References

1. Bolat C, Köse H. On The Properties of k-Fibonacci Numbers. *International Journal of Contemporary Mathematical Sciences*.2010; 22(5):1097-1105.
2. Çelik S, Durukan İ, Özkan E. New recurrences on Pell numbers, Pell-Lucas numbers, Jacobsthal numbers, and Jacobsthal-Lucas numbers. *Chaos, Solitons and Fractals*. 2021; 150: 111173.
3. Dikici R, Özkan E. An application of Fibonacci sequences in groups. *Applied Mathematics and Computation*. 2003; 136(2–3): 323-331.
4. Falcon S, Plaza A. On k-Fibonacci Sequences and Polynomials and their derivatives. *Chaos, Solutions and Fractals*. 2009; 39: 1005-1019.
5. Horadam A. F. A Generalized Fibonacci sequence. *Amer. Math. Montly*. 1961; 68(5): 827-232.
6. Koshy T. *Fibonacci and Lucas Numbers with Applications*. Canada: John Wiley & sons, inc.; 2001.
7. Koshy T. *Pell and Pell-Lucas Numbers with Applications*. New York: Springer, 2014.
8. Mikkawy M, Sogabe T. A New Family of k-Fibonacci numbers. *Applied Mathematics andand Computation*. 2010; 215: 4456-4461.
9. Öcal A. A., TugluN, Altinisik E. On the representation of k-generalized Fibonacciand Lucas numbers. *Applied Mathematics and Computation*. 2005; 170: 584-596.
10. Özkan E, Aydoğdu A, Altun İ. Some Identities for a Family of Fibonacci and Lucas Number. *Journal of Mathematics and Statistical Science*. 2017; 3(10): 295-303.
11. Özkan E, Altun İ. Generalized Lucas polynomials and relationships between the Fibonacci polynomials and Lucas polynomials. *Communications in Algebra*. 2019; 47(10): 4020-4030.
12. Özkan E, Aydın H, Dikici R. Applications of Fibonacci sequences in a finite nilpotent group. *Applied mathematics and computation*. 2003; 141 (2-3): 565-578.
13. Özkan E, Taştan M. On anew family of gauss k-Lucas numbers and their polynomials. *Asian-European Journal of Mathematics*. 2021; 14(6): 2150101.

14. Özkan E, Kuloğlu B. On the new Narayana polynomials, the Gauss Narayana numbers and their polynomials. *Asian-European Journal of Mathematics*. 2021; 14 (6): 2150100
15. Özkan E, Taştan M. k -Fibonacci Polynomials in The Family of Fibonacci Numbers. *Research&Reviews: Discrete Mathematical Structure*. 2019; 6(3): 19-22.
16. Özkan E, Taştan M, Aydoğdu A. 3-Fibonacci Polynomials in The Family of Fibonacci Numbers. *Erzincan University Journal of the Institute of Science and Technology*. 2019; 12(2): 926-933.
17. Özkan E, Taştan M, Aydoğdu A. 2-Fibonacci polynomials in the family of Fibonacci numbers. *Notes on Number Theory and Discrete Mathematics*. 2018; 24: 47-55.
18. Özkan E, Kuloğlu B. On A Jacobsthal-Like Sequence Associated with K - Jacobsthal-Lucas Sequence. *Journal of Contemporary Applied Mathematics*. 2020; 10 (2): 3-13.
19. Taştan M, Özkan E. The generalized k -Fibonacci polynomials and generalized k -Lucas polynomials. *Notes on Number Theory and Discrete Mathematics*. 2021; 27 (2): 148-158.

**A fractional mathematical model of tumor virus dynamics and treatment using
virotherapy**

Elif DENK¹, Seda İĞRET ARAZ²

¹Siirt University, Art and Science Faculty, Department of Mathematics, Siirt, Turkey

²Siirt University, Faculty of Education, Department of Mathematics Education, Siirt, Turkey

Abstract

Virotherapy is the cancer treatment that use a virus to find and destroy cancer cells without harming healthy cells. A mathematical model depicting such a process include the classes of infected tumor cells, uninfected tumor cells, effector T-cells and virions. To better understand and analyze this process, we solve this model with fractional differential operators. The numerical simulations for the considered model are performed for different values of fractional order.

Keywords: Tumor growth model, virotherapy, fractional derivative and integral, numerical scheme.

References

- [1] M. Caputo, M. Fabrizio, Applications of new time and spatial fractional derivatives with exponential kernels, *Progress in Fractional Differentiation and Applications*, 2 (2016), 1-11.
- [2] Atangana A., Baleanu D., Application of Fixed Point Theorem for Stability Analysis of a Nonlinear Schrodinger with Caputo-Liouville Derivative, *Filomat*, 31 (8), 2243.2248
- [3] Kim, Y., Magdalena, A.S., Othmer, H.G. 2007. "A hybrid model for tumor spheroid growth in vitro I: theoretical development and early results", *Math Models Methods Appl Sci.*, 17:1773–98.
- [4] Barillot, E., Calzone, L., Hupe, P., Vert, J.P., Zinovyev, A. 2013. "Computational systems biology of cancer", Boca Raton: CRC Press.
- [5] Watanabe, Y., Dahلمان, E., Hui, S. 2016, "A mathematical model of tumor growth and its response to single irradiation", *Theoretical Biology and Medical Modeling*, 13:6.

- [6] Igret Araz S., Numerical approximation with Newton polynomial for the solution of a tumor growth model including fractional differential operators, *Journal of Science and Technology* 2021, 14(1), 249-259 2021, 14(1), 249-259.
- [7] Abernathy Z., Abernathy K., Steven J., A mathematical model for tumor growth and treatment using virotherapy, *AIMS Mathematics*, 5(5): 4136–4150.
- [8] P. S. Kim, J. J. Crivelli, I. Choi, et al. Quantitative impact of immunomodulation versus oncolysis with cytokine-expressing virus therapeutics, *Math. Biosci. Eng.*, 12 (2015), 841–858.
- [9] Atangana A., Igret Araz S., *New Numerical scheme with Newton polynomial: Theory, methods and applications*, Elsevier, Academic press, 2021, ISBN:9780323854481.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Numerical solution of a fractional model of Covid-19 spread with non-total immunity

Bünyamin KORKMAZER¹, Seda İĞRET ARAZ²

¹Siirt University, Art and Science Faculty, Department of Mathematics, Siirt, Turkey

²Siirt University, Faculty of Education, Department of Mathematics Education, Siirt, Turkey

Abstract

In this study, we deal with the numerical solution of a mathematical model about Covid-19 spread including fractional differential operators that are power-law, exponential decay and Mittag-Leffler kernel. Model includes 5 classes which are susceptible, symptomatic, asymptomatic, recovered and death classes. Such model is solved by a numerical scheme based on Newton polynomial. The numerical simulations for this model are depicted for different values of fractional order.

Keywords: Covid-19 model, numerical scheme, fractional differentiation and integration.

References

- [1] M. Caputo, M. Fabrizio, Applications of new time and spatial fractional derivatives with exponential kernels, *Progress in Fractional Differentiation and Applications*, 2 (2016), 1-11.
- [2] Atangana A., Baleanu D., Application of Fixed Point Theorem for Stability Analysis of a Nonlinear Schrodinger with Caputo-Liouville Derivative, *Filomat*, 31 (8), 2243.2248
- [3] Atangana A., Igret Araz S., Nonlinear equations with global differential and integral operators: Existence, uniqueness with application to epidemiology. *Results in Physics*, 103593, 2020.
- [4] Atangana A., Igret Araz S., Modeling and forecasting the spread of Covid-19 with stochastic and deterministic approaches: Africa and Europe, *Advances in Difference Equations*, 2020.

- [5] Zakary O., Bidah S., Rachik M, Ferjouchia H., Mathematical Model to Estimate and Predict the Covid-19 Infections in Morocco: Optimal Control Strategy, Journal of Applied Mathematics, 2020.
- [6] Igrat Araz S., Analysis of a Covid-19 model: Optimal control, stability and simulations. AlexandriaEngineering Journal, 60 (1), 2020.
- [7] Adiga A., Dubhashi D., Lewis B., Marathe M., Venkatramanan S., Vullikanti A., Mathematical Models for Covid-19 Pandemic: A Comparative Analysis, Journal of the Indian Institute of Science, volume 100, 793.807, 2020.
- [8] Atangana A., Araz SI., Mathematical model of Covid-19 spread in Turkey and South Africa: Theory, methods and applications, Advances in Difference Equations, 2021.
- [9] Khan MA., A Atangana, Alzahrani E., The dynamics of Covid-19 with quarantined and isolation, Advances in Difference Equations 2020 (1), 1-22.
- [10] Thabet STM., Abdo MS., Shah K., Abdeljawat T., Study of transmission dynamics of Covid-19 mathematical model under ABC fractional order derivative, Results in Physics, 19(2020), 2020.
- [11] Gao W., Baskonus HM., Shi L., New investigation of Bats-HostsReservoir-People coronavirus model and apply to 2019-nCoV system, Advances in Difference Equations, 2020(391), 1-11, 2020.
- [12] Atangana A., Igrat Araz S., New Numerical scheme with Newton polynomial: Theory, methods and applications, Elsevier, Academic press, 2021, ISBN:9780323854481.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Transfer Functions by New General Integral Transform

Ali Akgül

Siirt University, Art and Science Faculty, Department of Mathematics, 56100 Siirt, Turkey

aliakgul@siirt.edu.tr

Abstract

In this work, we apply the new general integral transform to obtain the Transfer functions. The obtained Transfer functions are new in the literature. Therefore, they will be very useful for mathematicians and engineers. We use power-law, exponential-decay and Mittag-Leffler kernels.

We present the applications of the circuit problems by the new general integral transform. In the circuit problems, we check the effect of the three different kernels. We demonstrate the numerical simulations to prove the efficiency of the general integral transform. We use many integral transforms and obtain very interesting transfer functions.

References

- [1] A. Akgül, A novel method for a fractional derivative with non-local and non-singular kernel, *Chaos, Solitons and Fractals* 114 (2018) 478–482.
- [2] E.K. Akgül, Solutions of the linear and nonlinear differential equations within the generalized fractional derivatives, *Chaos* 29, 023108 (2019).
- [3] A. Atangana and D. Baleanu, New fractional derivatives with nonlocal and non-singular kernel, theory and application to heat transfer model, *Thermal Science*, 20 (2016) 763-769.
- [4] A. Atangana, Non validity of index law in fractional calculus: A fractional differential operator with Markovian and non-Markovian properties, *Physica A* 505 (2018) 688-706.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

**The cubic B-spline polynomials approach for numerical solutions of Bagley-Torvik and
Painlevé differential equations involving the Caputo-Fabrizio derivative**

Omar Abu Arqub ^{1,*}, Ahlem Ben Rabah ²

¹ Department of Mathematics, Al-Balqa Applied University, Salt 19117, Jordan

² Department of Mathematics, Faculty of Science, The University of Jordan, Amman 11942,
Jordan

*Corresponding author: Omar Abu Arqub, e-mail: o.abuarqub@bau.edu.jo

Abstract

In this present article, the well-known Bagley--Torvik equation, which is a special kind of fractional differential equations and Painlevé equations which have a significant role in fractional calculus are solved by cubic B-spline polynomials which are utilized as basis functions in a collocation plan. Applying the collocation points, defining the desired solution and its fractional derivative which is it in the Caputo-Fabrizio sense in sum forms, and matrix operations, our improved proposed technique transforms the initial value problem for the Bagley--Torvik and Painlevé fractional differential equations into a scheme of linear and nonlinear algebraic equations. The accuracy, convergence rate, and computational complexity of the scheme are analyzed based on a large number of independent runs and their comprehensive statistical analysis. The comparative studies of the results obtained are made with Mathematica11 solutions.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Reliable Structure Preserving Numerical Analysis of Epidemic Models

Muhammad Rafiq¹

¹Department of Mathematics, Faculty of Sciences, University of Central Punjab,
Lahore, Pakistan

E-mail: m.rafiq@ucp.edu.pk

Abstract

The models for transmission dynamics of infectious diseases are non-linear and hard to solve analytically. Some authors proposed semi-analytic and exact solutions of epidemic models. These solutions have some serious flaws and do not exhibit the true dynamics of an infectious disease in a population. In this work, a reliable numerical analysis for epidemic models is presented which preserves all the essential features of the continuous model. The proposed numerical analysis remains consistent with the biological nature of epidemic models in all scenarios.

Keywords: Epidemic Model; Exact Solution; Numerical Analysis; Structure Preserving

,

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Applications of Lie groups and Lie algebras in numerical methods

Mir Sajjad Hashemi¹

¹Department of Mathematics, Basic Science Faculty, University of Bonab, P.O. Box 55513-
95133, Bonab, Iran.

Email: hashemi_math396@yahoo.com

Abstract

Differential equations play an important role in applied mathematics and are omnipresent in the sciences and in technical applications. They appear in many different fields such as chemical reaction kinetics, molecular dynamics, electronic circuits, population dynamics, control theory and astrodynamical problems, to name just a few. However, since the early days of the subject, it has become evident that very often finding closed solutions is either simply impossible or extremely difficult. Therefore, computing or approximating solutions of differential equations, fractional, partial as well as ordinary, linear or nonlinear, constitutes a crucial ingredient in all mathematical sciences. Very often in applications, the differential equation modeling the physical phenomenon one aims to study possesses qualitative (geometric) properties that are absolutely essential to preserve under discretization. Starting from the case of symplectic integration, the search for numerical integration methods that preserve the geometric structure of the problem was generalized to other types of differential equations possessing a special structure worth being preserved under discretization. Examples include volume preserving systems, differential equations defined in Lie groups and homogeneous manifolds, systems possessing symmetries or reversing symmetries, etc. In this talk, we present some novel geometric numerical integration techniques which can be developed for many other kind of differential equations.

Keywords: Numerical method, Geometric integration, Lie group, Lie algebra.

References

1. Hashemi, M.S., Darvishi, E., Baleanu, D., A geometric approach for solving the density-dependent diffusion Nagumo equation, *Advances in Difference Equations* **2016 (1)**, 1-13 (2016).
2. Hashemi, M.S., Baleanu, D., Lie symmetry analysis of fractional differential equations, *CRC Press* (2020).
3. Hashemi, M.S., Inc, M., Yusuf, A., On three-dimensional variable order time fractional chaotic system with nonsingular kernel, *Chaos, Solitons & Fractals* **133**, 109628 (2020).
4. Hashemi, M. S.; Akgül, A., Solitary wave solutions of time-space nonlinear fractional Schrodinger's equation: Two analytical approaches, *JOURNAL OF COMPUTATIONAL AND APPLIED MATHEMATICS* **339**, 147-160 (2018).
5. Hashemi, M.S., Some new exact solutions of (2+1)-dimensional nonlinear Heisenberg ferromagnetic spin chain with the conformable time fractional derivative, *OPTICAL AND QUANTUM ELECTRONICS* **50(2)**, 1-11 (2018).
6. Hashemi, M.S., A novel approach to find exact solutions of fractional evolution equations with non-singular kernel derivative, *Chaos, Solitons & Fractals* **152**, 111367 (2021).

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

**Optimal balls of classical and stochastic systems of nonlinear partial differential
equations**

Muhammad Sajid Iqbal¹

¹Department of Mathematics and Statistics, The University of Lahore, Pakistan

Abstract

The solutions of nonlinear partial differential equations (PDEs), in general, lie in the function spaces. The presence of chaos or noise in a PDE leads to the loss of the usual regularity properties. The current research provides the junction of exact solutions and the a-priori explicit estimates describing the maximum length of continuity of solutions of under nonlinear dynamical problems for stochastic PDEs. Another contribution is the common continuity of the solution of underlying system of nonlinear partial differential equations.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Common fixed points technique in complex valued b-metric spaces

Liliana Guran¹, Monica Felicia Bota²

Abstract

In this paper, we introduce fixed theorem for a general contractive condition in complex valued b-metric spaces. Also some corollaries under this contractive condition are obtained. As applications, we give a section applying our results in the case on integral type contractions. Moreover, we find a unique solution for Urysohn integral type equations system and an illustrative example is given to support our obtaining results. Our results extend and generalize the results of Rao et. al. [7] and some known results in the literature.

References

- [1] I. Arandjelović, Z. Radenović, S. Radenović, *Boyd-Wong-type common fixed point results in cone metric spaces*, Appl. Math. Comput., 217 (2011), 7167-7171.
- [2] A. Azam, B. Fisher, M. Khan, *Common Fixed Point Theorems in Complex Valued Metric Spaces*, Numerical Functional Analysis and Optimization, 32:3(2011), 243-253, DOI: 10.1080/01630563.2011.533046.
- [3] D. W. Boyd, J. S. W. Wong, *On nonlinear contractions*, Proc. Amer. Math. Soc., 20 (1969), 458-464.
- [4] S. Bhatt, S. Chaukiyal, R. C. Dimri, *A common fixed point theorem for weakly compatible maps in complex valued metric spaces*, Int. J. Math. Sci. Appl., 1 (3) (2011), 1385-1389.
- [5] S. K. Datta, S. Ali, *A common fixed point theorem under contractive condition in complex valued metric spaces*, Int. J. Advanced Scientific and Technical Research, 2 (6) (2012),

467-475.

- [6] A. K. Dubey, *Complex valued b-metric spaces and common fixed point theorems under rational contractions*, J. Complex Anal., 2016 (2016), 1-7.
- [7] K. P. R. Rao, P. R. Swamy, J. R. Prasad, *A common fixed point theorem in complex valued b-metric spaces*, Bulletin of Mathematics and Statistics Research., 2013, 1.
- [8] N. Singh, D. Singh, A. Badal, V. Joshi, *Fixed point theorems in complex valued metric spaces*, J. Egyptian Math. Soc., 24 (2016), 402-409.
- [9] W. Sintunavarat, P. Kumam, *Generalized common fixed point theorems in complex valued metric spaces and applications*, J. Inequality Appl., 2012 (1) (2012), 1-12.
- [10] W. Sintunavarat, J. C. Yeol, P. Kumam, *Urysohn integral equations approach by common fixed points in complex valued metric spaces*, Adv. Diff. Equ., 2013 (2013), 1-14.

LILIANA GURAN,

VASILE GOLDI, S WESTERN UNIVERSITY OF ARAD, ROMANIA.,

Email address: guran.liliana@uvvg.ro.

MONICA FELICIA BOTA,

DEPARTMENT OF MATHEMATICS, BABE, S-BOLYAI UNIVERSITY, CLUJ-NAPOCA, ROMANIA.,

Email address: monica.bota@ubbcluj.ro.

2010 *Mathematics Subject Classification.* 47H10; 54H25.

Key words and phrases. fixed point, common fixed point, complex valued b-metric space, Urysohn integral equations system.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Application of Fractional Order Techniques on Diabetes Model

Dr. Muhammad Farman

Department of Mathematics and Statistics, University of Lahore, Lahore-54590, Pakistan.

Abstract:

We formulate a fractional-order mathematical model for the populations of diabetic patients consist three-compartment G , X , and I . The fractal-fractional diabetes Model is investigated with the ABC technique using Sumudu transform, Atangana-Toufik techniques for normal and type type-1 diabetes. Also, the deterministic mathematical model for diabetes mellitus is investigated with the effect of the fractional parameters. Solutions are derived to investigate the influence of fractional operator which shows the impact of the disease for type-1 diabetes. The existence and uniqueness results of the fractional-order model are derived using fixed point theory. Also, an error analysis has been made for the proposed scheme. We suggest an impulsive differential equation model study plasma glucose control for diabetic patients with impulsive insulin injections. It is regarded as a deterministic mathematical model related to the diabetes mellitus fractional derivatives. Simulation has been made for developed solutions of fractional order diabetes model to check the actual behavior of a normal person as well as a type-1 diabetes patient. The results of these case studies indicate that this plasma glucose control of the fractional-order model is an appropriate candidate.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Numerical Analysis of a Non-Linear Stochastic Epidemic Model

Ali Raza

Department of Mathematics, National College of Business Administration &
Economics, Lahore, Pakistan

Department of Mathematics, Govt. Maulana Zafar Ali Khan Graduate College Wazirabad,
Punjab Higher Education Department Lahore, Pakistan

*E-mail: alimustasamcheema@gmail.com

Abstract

The nature of epidemic growth and spread is inherently random due to the unpredictability of person-to-person contacts. It is essential to include this randomness in models for emerging infectious diseases. Stochastic models could be a more appropriate way of modeling epidemics in many circumstances. The Euler Maruyama, Milstein, and many more methods are widely used in literature to solve highly nonlinear stochastic differential equations (SDE's). Unfortunately, the methods mentioned above are not reliable for restoring the structure of the continuous model's positivity, boundedness, and dynamical consistency. Moreover, these methods are not consistent with the nature of biological properties. So, to overcome these issues, the proposed numerical method, like the non-standard finite difference in the sense of stochastic, is designed to preserve the continuous model's structure and remain consistent with its biological nature.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Dynamical Behaviour of Smoking Model

Anwar Zeb¹

¹Department of Mathematics, COMSATS University Islamabad, Abbottabad Campus,
Pakistan

Abstract

In this talk, first, we present a new smoking mathematical model for which the interaction term is the square root of potential and occasional smokers. Then discuss the local and global stability of proposed model. Finally, show the numerical results graphically.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Analysis of system of differential equations

Nourhane Attia

Abstract

In the present research, a system of fractional differential equations has been examined with the help of reproducing kernel Hilbert space method. This important fractional model helps us to understand the interaction between the predator and prey. We make use of the Caputo fractional derivative. The technique employed to construct new numerical solutions for the considered model, which is presented as a system of two fractional ordinary differential equations. The solution methodology is based on the use of two important Hilbert spaces, as well as on the construction of a normal basis through the use of the Gram-Schmidt orthogonalization process. The computational results show the effect of the fractional derivative in the obtained results the superior performance of the proposed method.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Fractional stochastic inequalities involving p-convex stochastic process

Auwalu Hamisu Usman, Usa Wannasingha Humphries

Abstract

The main objective of this article is to derive a new fractional refinement of Hermite-Hadamard's inequality using p-convex stochastic processes essentially involving a new generalized stochastic mean-square fractional integrals. A new identity involving generalized stochastic mean-square fractional integrals is obtained. Using this identity some new estimates of upper bounds involving p-convex stochastic processes are also obtained. 2010 Mathematics Subject Classification: 26A51, 26D15, 26A33.

Keywords: p-convex stochastic processes, inequality, fractional, Hermite-Hadamard

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

**Numerical Solutions of a Heat Transfer for Fractional Maxwell Fluid Flow with Water
Based Clay Nanoparticles; A Finite Difference Approach**

Muhammad Imran Asjad

Abstract

Fractional-order mathematical modeling of physical phenomena is the hot topic among the researcher because it has many advantages over the positive integer mathematical modeling. In this context, the appropriate solutions of such fractional-order physical modeling become a challenging task among scientists. This paper presents the study of unsteady free convection fluid flow and heat transfer of Maxwell with the presence of Clay nanoparticle modeling using fractional calculus. The obtained model transformed into a set of linear non-dimensional partial differential equations (PDEs). The finite difference scheme proposed to discretize the obtained set of non-dimensional PDEs. Maple code was developed and executed against the physical parameters and fractional-order parameters in order to see the behavior of velocity and temperature profiles. Some limiting solutions are obtained and compared with the latest existing ones in literature. The comparative study witnesses that the proposed scheme is a very efficient tool to handle such a physical model and can be extended to more diversified problems of complex nature.

Keywords: Numerical method; Fractional Calculus; Nanoparticles; Maxwell fluid; Heat transfer

Weber-Type Integral Transform Connected with Robin-Type Boundary Conditions

Nehad Ali Shah

Abstract

A new Weber-type integral transform and its inverse are defined for the representation of a function $f(r,t), (r,t) \in [R,1] \times [0,\infty)$ that satisfies the Dirichlet and Robin-type boundary

conditions $f(R,t) = f_1(t)$, $f(1,t) - \alpha \left. \frac{\partial f(r,t)}{\partial r} \right|_{r=1} = f_2(t)$, respectively.

The orthogonality relations of the transform kernel are derived by using the properties of Bessel functions. The new Weber integral transform of some particular functions has been determined. The integral transform defined is a suitable tool for determining analytical solutions of the transport problems with sliding phenomena that often occur into flows through micro channels, pipes or blood vessels.

**Academia International Conference on Mathematics and Mathematics Education, 1-3
December 2021, Siirt, TURKEY**

Application of fractional derivatives

Harendra Singh

Abstract

In this lecture, we will discuss about the different types of fractional derivatives. We will compare these derivatives and show which one is better in compare to the other. We will also discuss some applications of fractional derivatives in science and engineering.